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WP BAILEY PAIRS AND DOUBLE SERIES IDENTITIES

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Abstract: In this paper, using WP Bailey pairs and conjugate WP Bailey pairs, certain double series identities have been established.

Keywords and Phrases: WP Bailey pairs, WP Conjugate Bailey pairs, transformation formula, summation formula, basic hypergeometric series.

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1. Introduction

We begin by recalling some standard notations and terminology. Let a and q be complex numbers with |q| < 1. Then the q- shifted factorial is defined by

$$(a;q)_0 = 1, (a;q)_n = (1-a)(1-aq)...(1-aq^{n-1}), n \in \mathbb{N} \text{ and } (a;q)_\infty = \prod_{r=0}^\infty (1-aq^r).$$

Also, for the sake of brevity, we often write

$$(a_1, a_2, ..., a_r; q)_n = (a_1; q)_n (a_2; q)_n ... (a_r; q)_n.$$

The basic q- hypergeometric series is defined by

$${}_{r}\Phi_{s}\left[\begin{array}{c}a_{1},a_{2},...,a_{r};q;z\\b_{1},b_{2},...,b_{s}\end{array}\right]=\sum_{n=0}^{\infty}\frac{(a_{1},a_{2},...,a_{r};q)_{n}z^{n}}{(q,b_{1},b_{2},...,b_{s};q)_{n}}\left\{(-)^{n}q^{n(n-1)/2}\right\}^{1+s-r}$$